

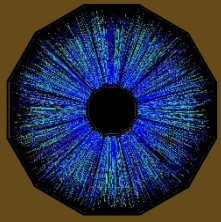
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# CME Focus Group

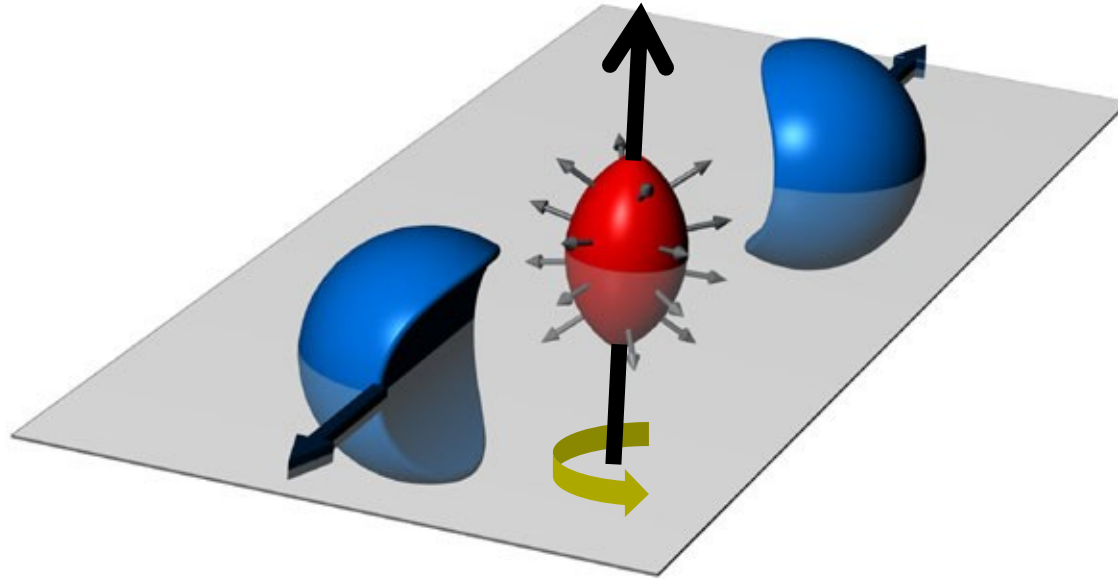
(updated with a new figure and a backup slide)

Jim Thomas

February 17<sup>th</sup>, 2023

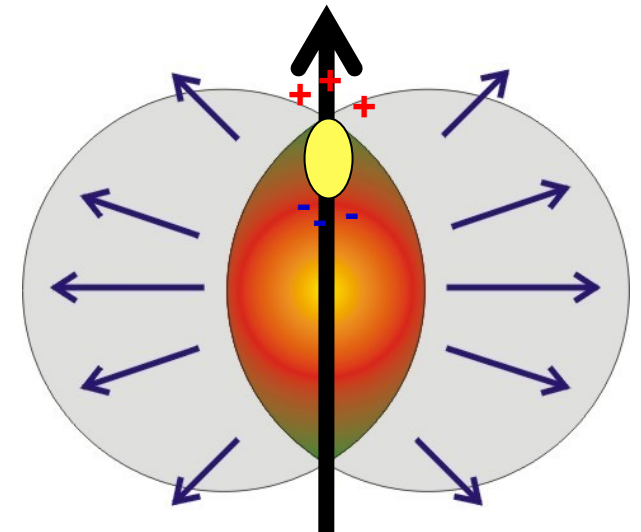
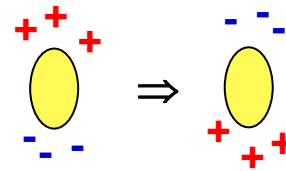


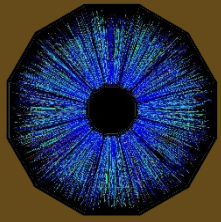
# CME: Separation of Charge with respect to the reaction plane



- If a chirally restored bubble is created in a heavy ion collision, the positively charged quarks will go up ... then hadronize ... and yield an excess of positive pions above the plane
- Unfortunately, it could be just the opposite in the next event depending on the topological charge in the bubble

- The signal is manifestly odd  
 $x \Rightarrow -x$  ,  $p \Rightarrow -p$   
but the observable will be even
- The charge-flow asymmetry is too small to be seen in a single event but may be observable with correlation techniques





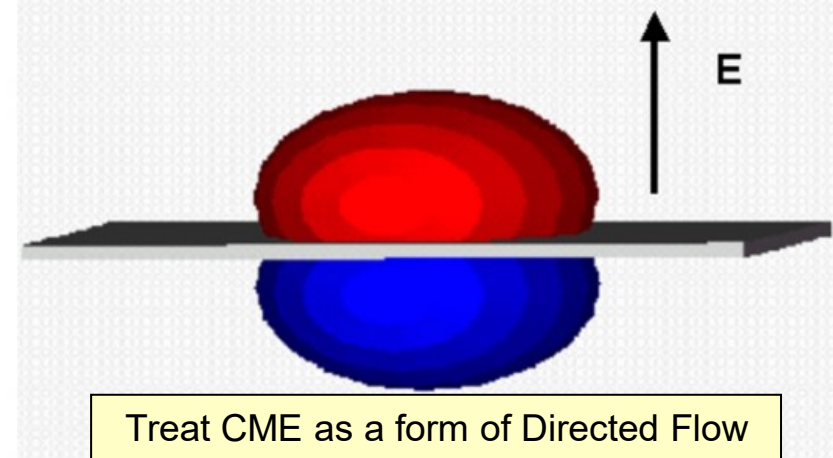
# The observable and the tools for analysis

$n=1$ : Directed Flow has a period of  $2\pi$  (only one maximum)

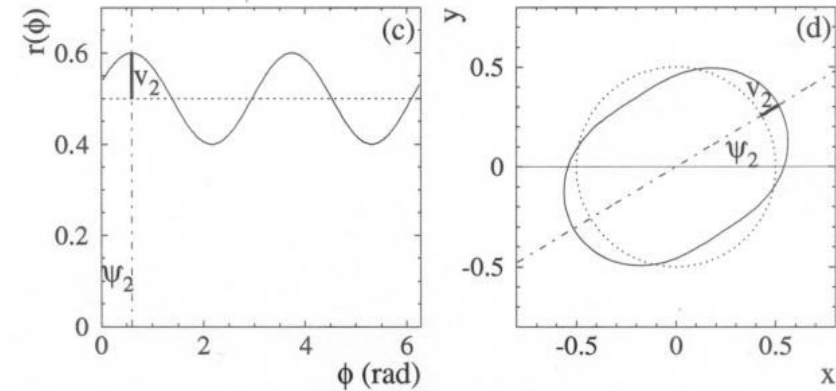
- $v_1$  measures whether the flow goes to the left or right – whether the momentum goes with or against a billiard ball like bounce. For collisions of identical nuclei, symmetry forces  $v_1$  to be an odd function of  $\eta$

$n=2$ : Elliptic flow has a period of  $\pi$  (two maximums)

- $v_2$  represents the elliptical shape of the momentum distribution. It is an even function of  $\eta$  for identical nuclei



Treat CME as a form of Directed Flow



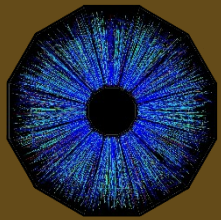
sin() terms may be non-zero if parity isn't conserved

Perform a Fourier Transform to isolate the coefficients

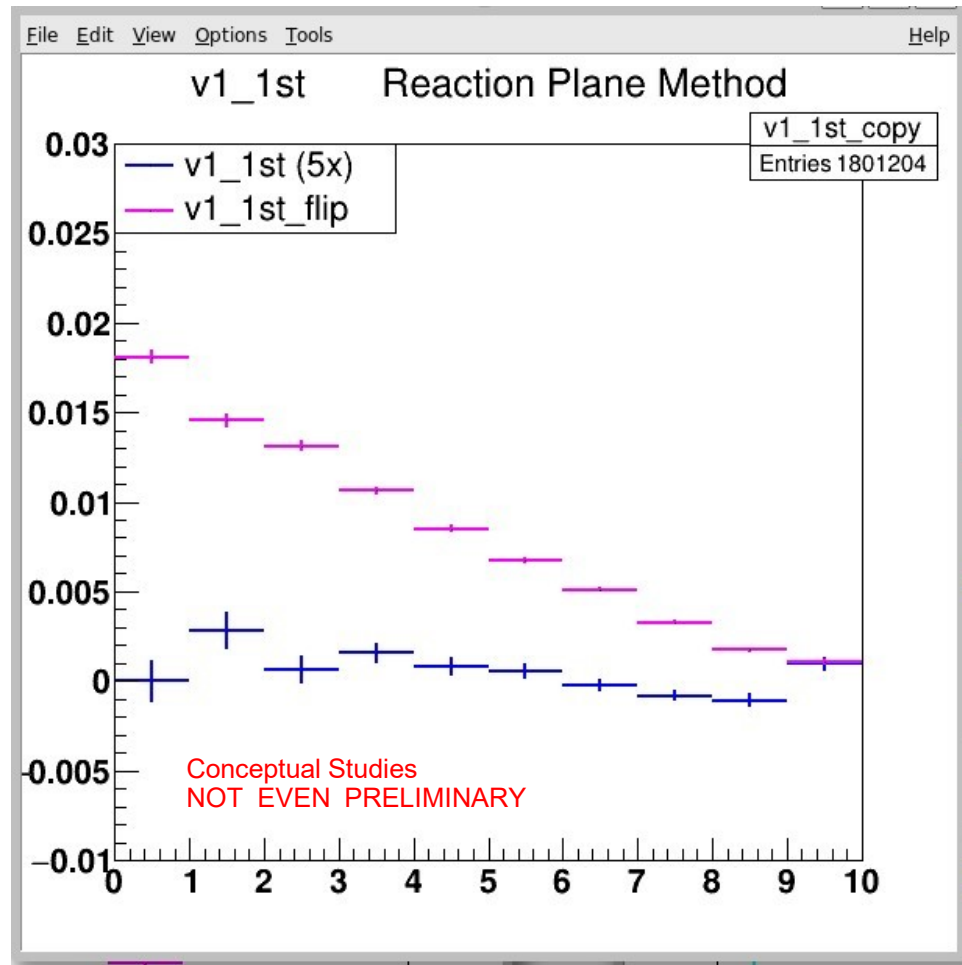
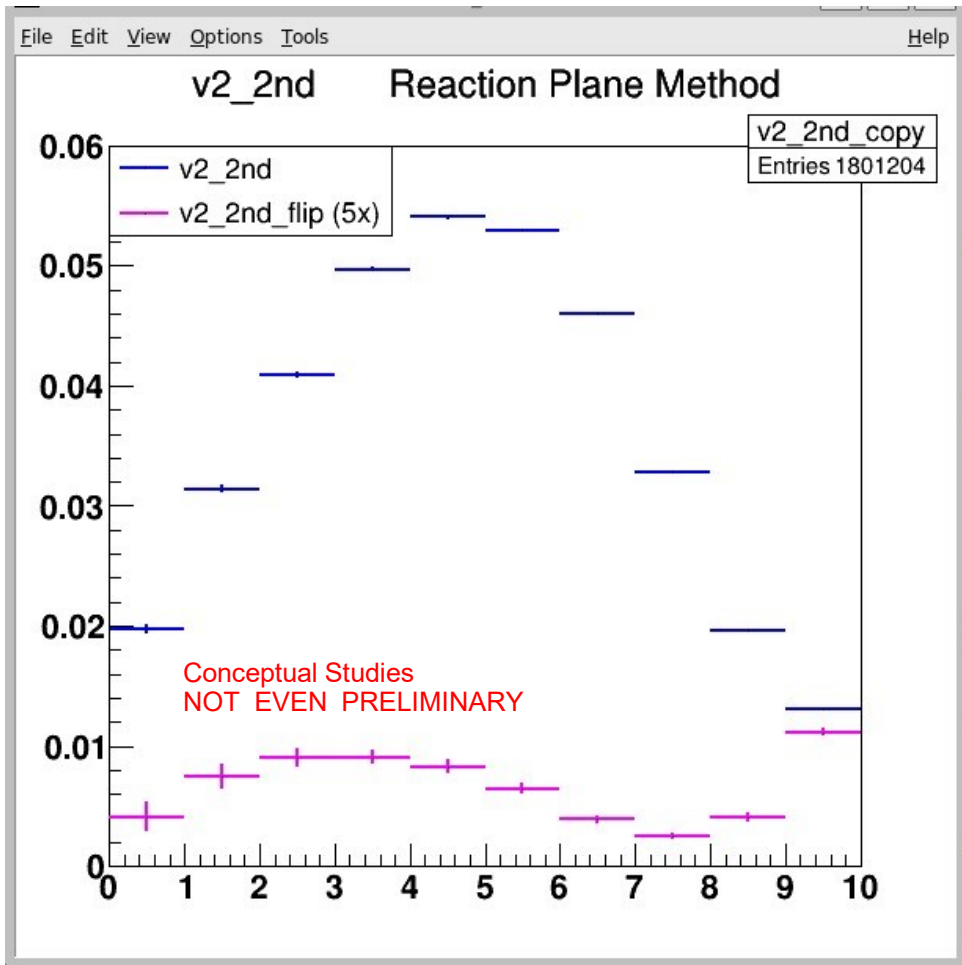
$$E \frac{dN^3}{d^3p} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} ( 1 + 2a_1 \sin(\Delta\phi) + 2v_1 \cos(\Delta\phi) + 2a_2 \sin(2\Delta\phi) + 2v_2 \cos(2\Delta\phi) + 2v_4 \cos(4\Delta\phi) + \dots )$$

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↑
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isotropic
parity non-conserving
directed
h.o. nc terms
elliptic
higher order terms

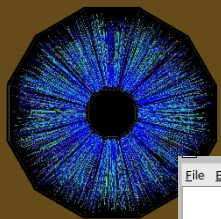


# $v_1$ and $v_2$ in Au-Au 200 GeV (~1 Million events from Run 19)



$v_1$  and  $v_2$  doing familiar things (Note:  $\Psi_1$  &  $\Psi_2$  RPs measured in TPC)

# Several more low order terms ...

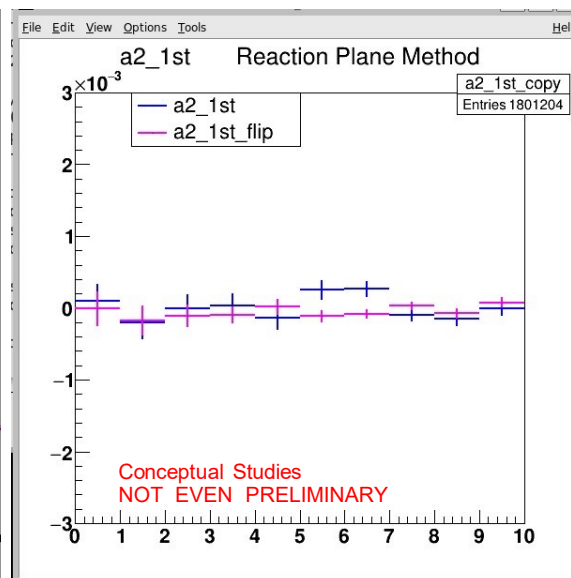
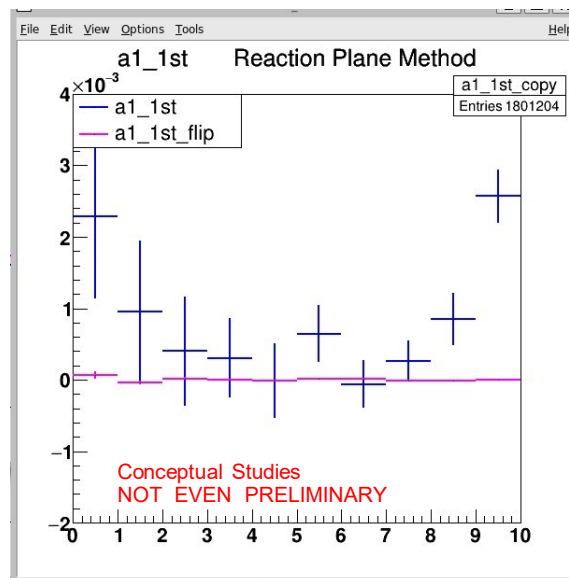
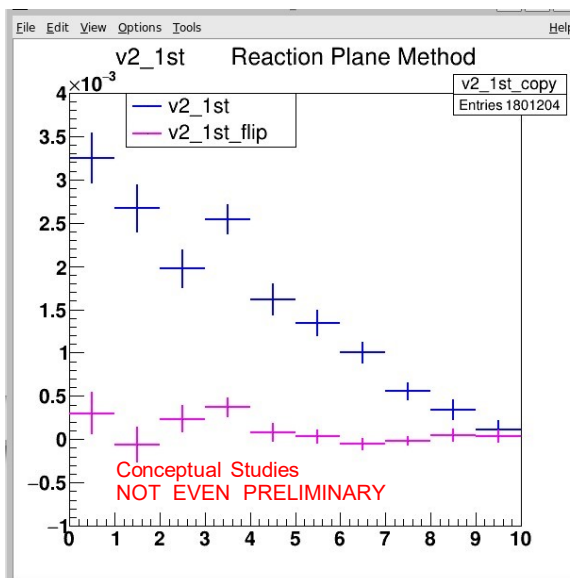
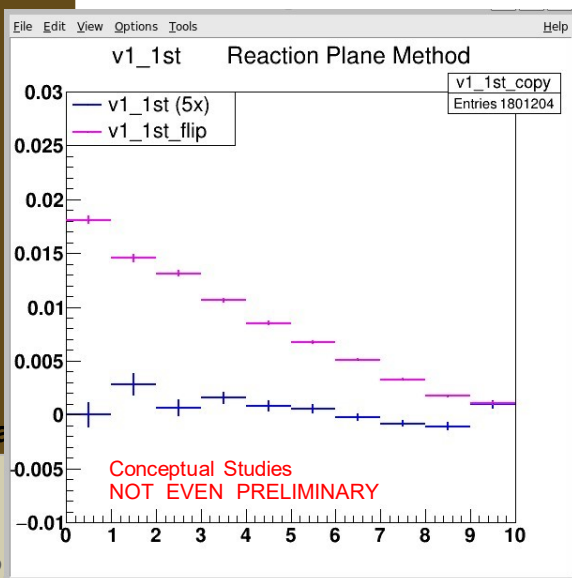
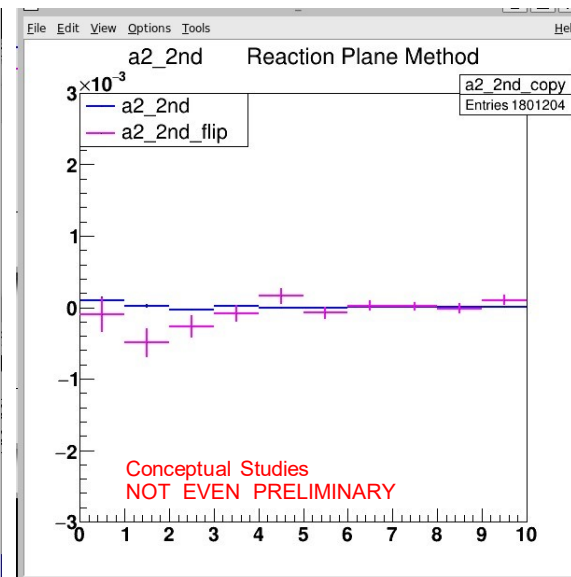
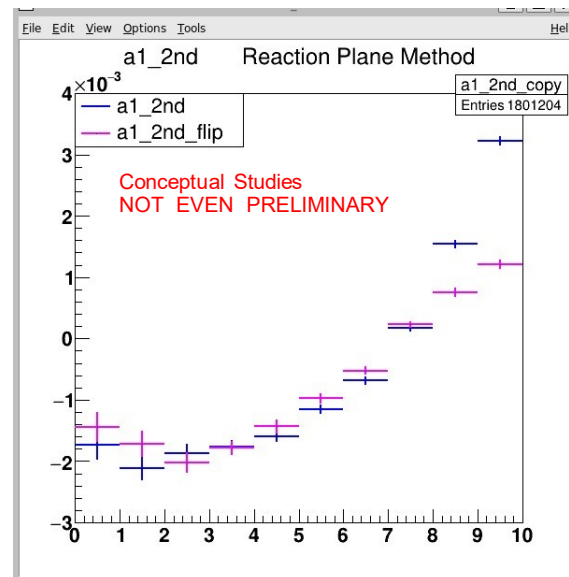
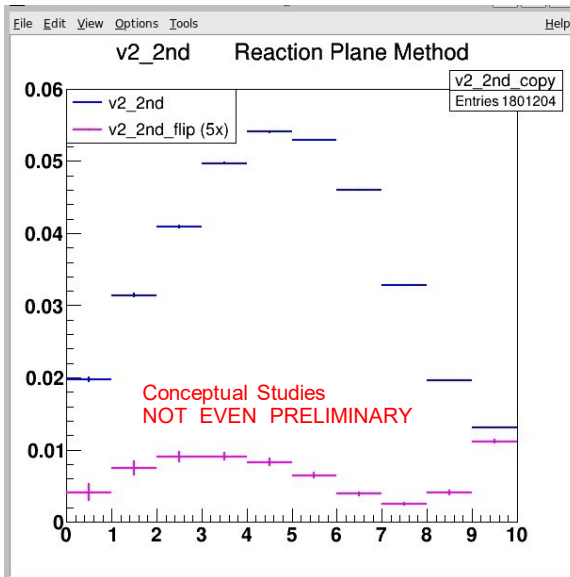
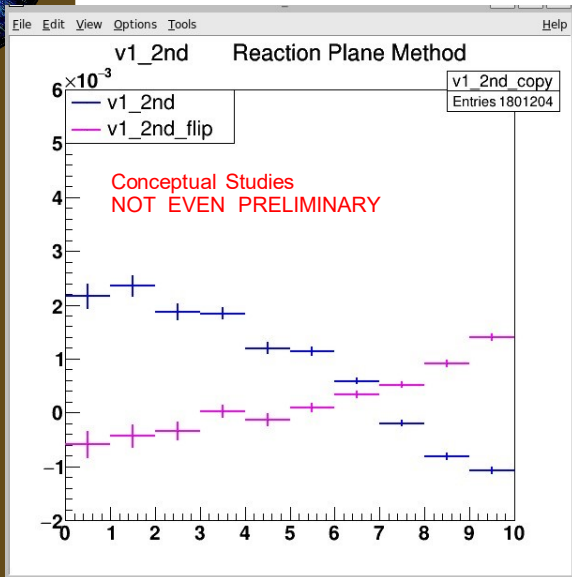


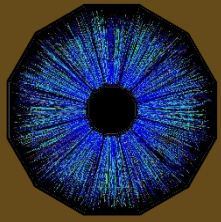
## The Chiral Magnetic Effect

Jim Thomas

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17-Feb-2



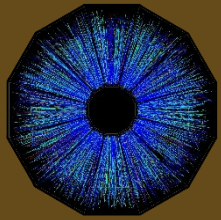


## The $\gamma$ observable

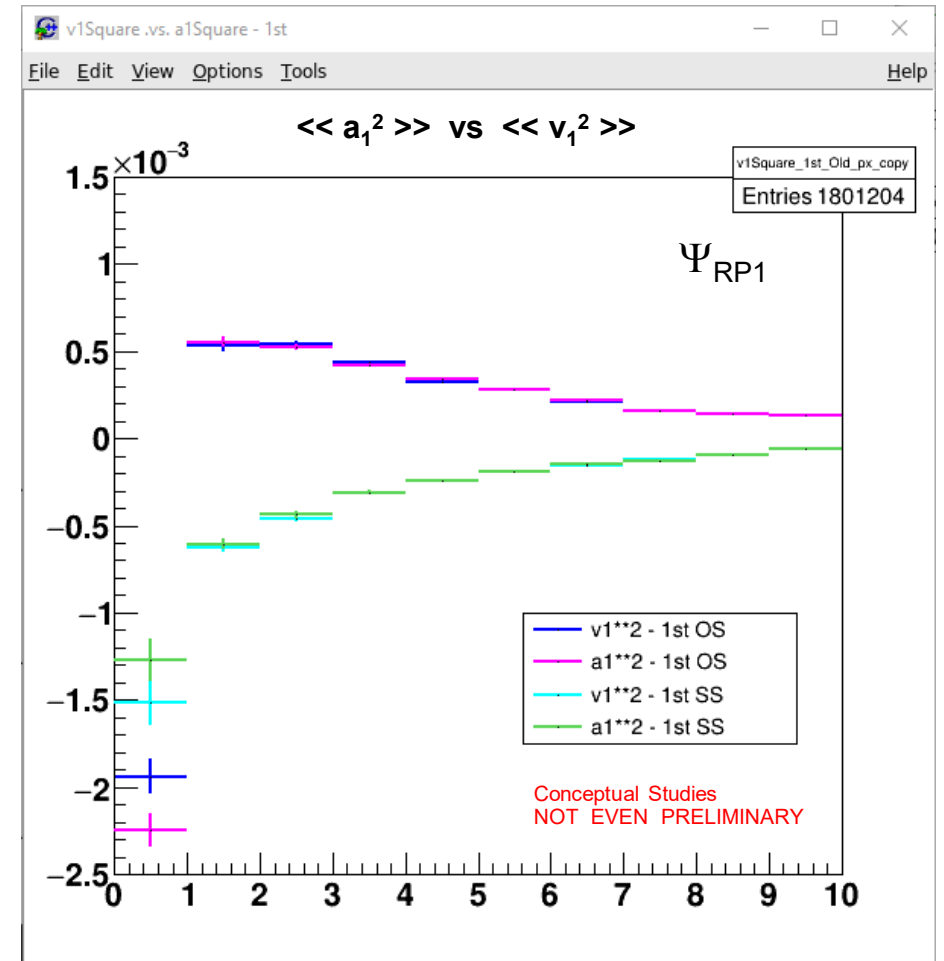
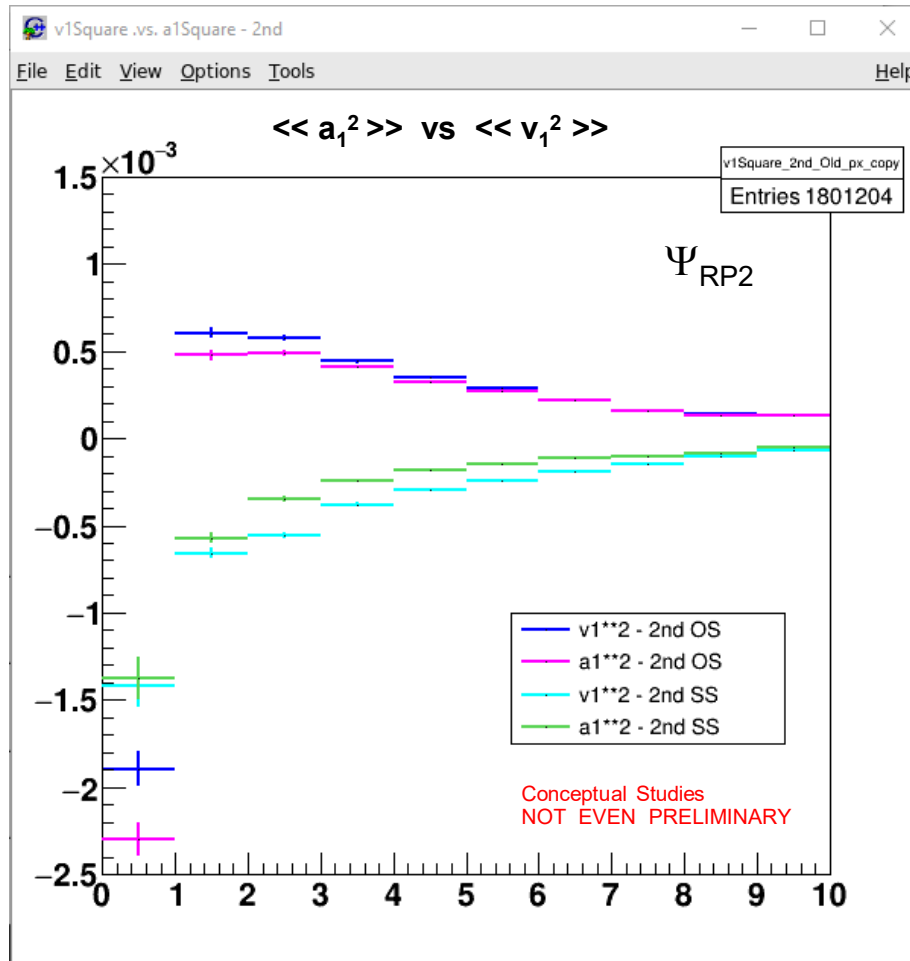
- The coefficients of the Fourier expansion for the invariant yield are

$$v_n \equiv \langle \cos(n(\varphi - \Psi_R)) \rangle \quad \text{or} \quad v_n^2 = \langle \cos(n(\varphi_i - \varphi_j)) \rangle$$

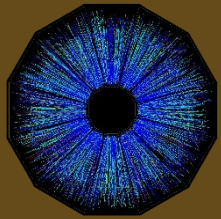
- where the average is taken over all particles in the event and  $\Psi_R$  is the known reaction plane angle (e.g. from the TPC or the EPD)
- The equation on the right is a multi particle correlation
- Under certain assumptions  $v_1$  is directed flow
  - Note that ‘normal’  $v_1$  measurements in a symmetric Au-Au collision have an intrinsic symmetry that requires weighting by  $\text{sign}(\eta)$  to measure  $v_{1 \text{ Hydro}}$
  - Tool: look for charge flow (up/down) without  $\text{sign}(\eta)$  weighting because  $v_{1 \text{ Hydro}}$  will cancel out if we have symmetric  $\eta$  acceptance.
- $\gamma$  is a clever observable. A triple correlation  $\Rightarrow \langle \cos(\phi_i + \phi_j - 2\phi_k) \rangle$ 
  - Mixed Harmonics:  $\langle \cos(\varphi_i - \varphi_k) \cos(\varphi_j - \varphi_k) - \sin(\varphi_i - \varphi_k) \sin(\varphi_j - \varphi_k) \rangle = (v_1^2 - a_1^2) v_2 + \dots$
  - A good candidate to measure charge sensitive flow since  $v_1 \Rightarrow 0$  and hopefully  $v_{1\_bkgd}$  ( $\sim$ in-plane bkgd) cancels  $a_{1\_bkgd}$  ( $\sim$ out of plane bkgd), thus:  
$$(v_1^2 - a_1^2) * v_2 \Rightarrow -a_1^2 * v_2$$
  - Should work well when  $v_1$  is small and  $v_2$  is large



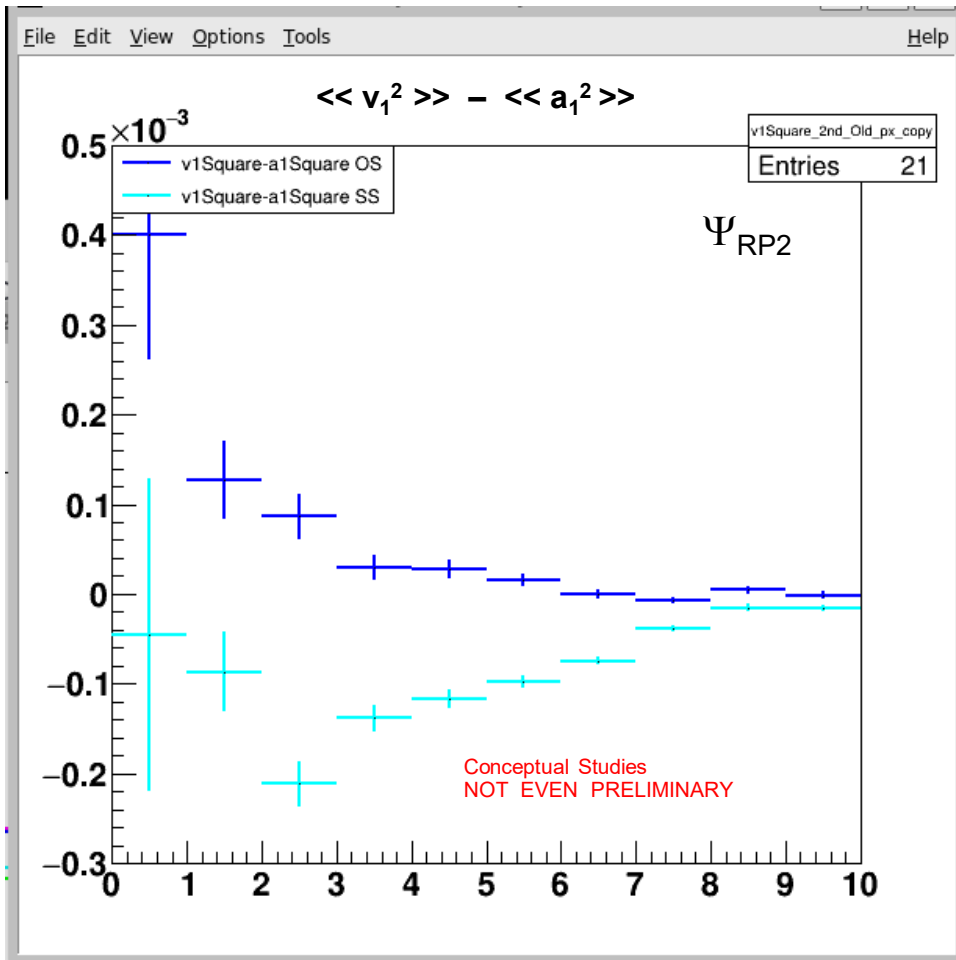
# $a_1^2$ and $v_1^2$ from the 200 GeV Au-Au Run 19



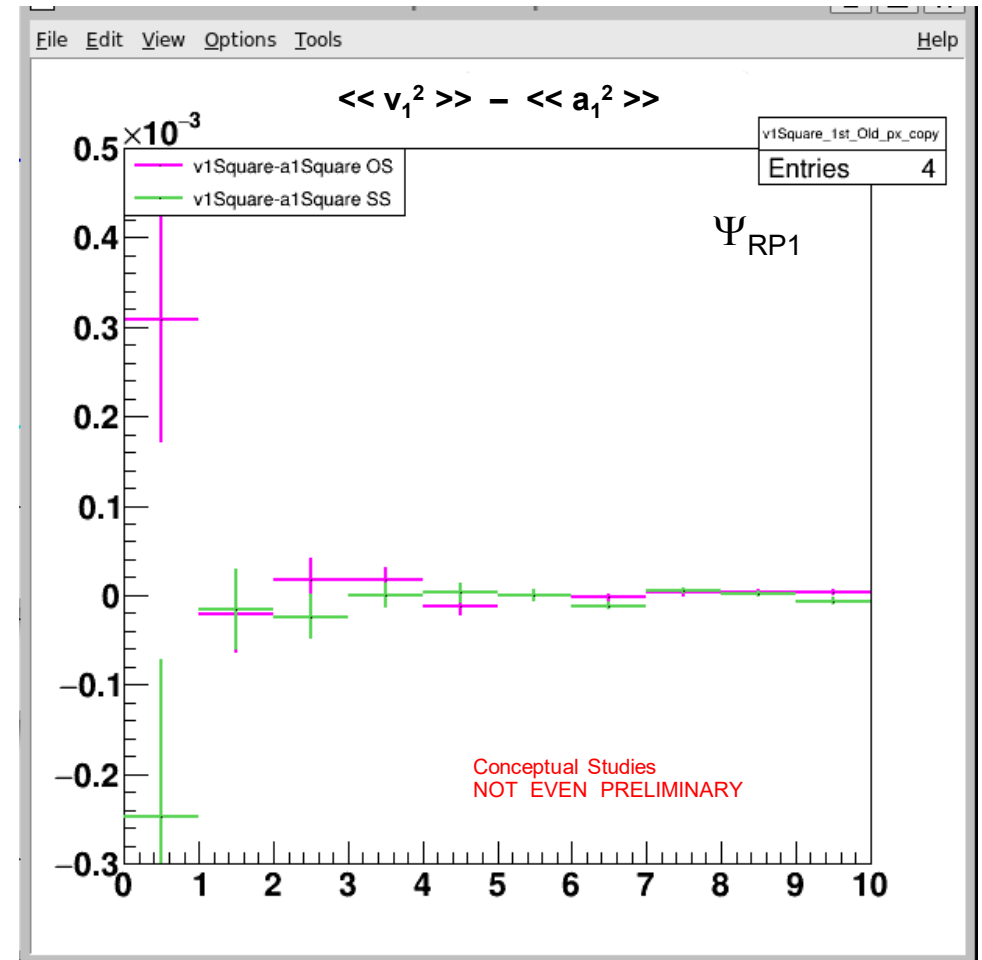
- The notation  $a_1^2$  denotes the EbyE quantity  $\Sigma (a_{1,p1} * a_{1,p2})$  with  $p1 \neq p2$
- $a_1^2$  is similar in shape and magnitude to  $v_1^2$ , independent of which RP is used in the study
- $a_1^2$  shows charge separation ... but so does  $v_1^2$  ... I didn't expect to see that



# $a_1^2$ and $v_1^2$ from the 200 GeV Au-Au Run 19

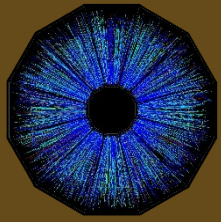


$(v_1^2 - a_1^2)$  with  $\Psi_{RP2}$  suggests that  $SS < 0, OS > 0$



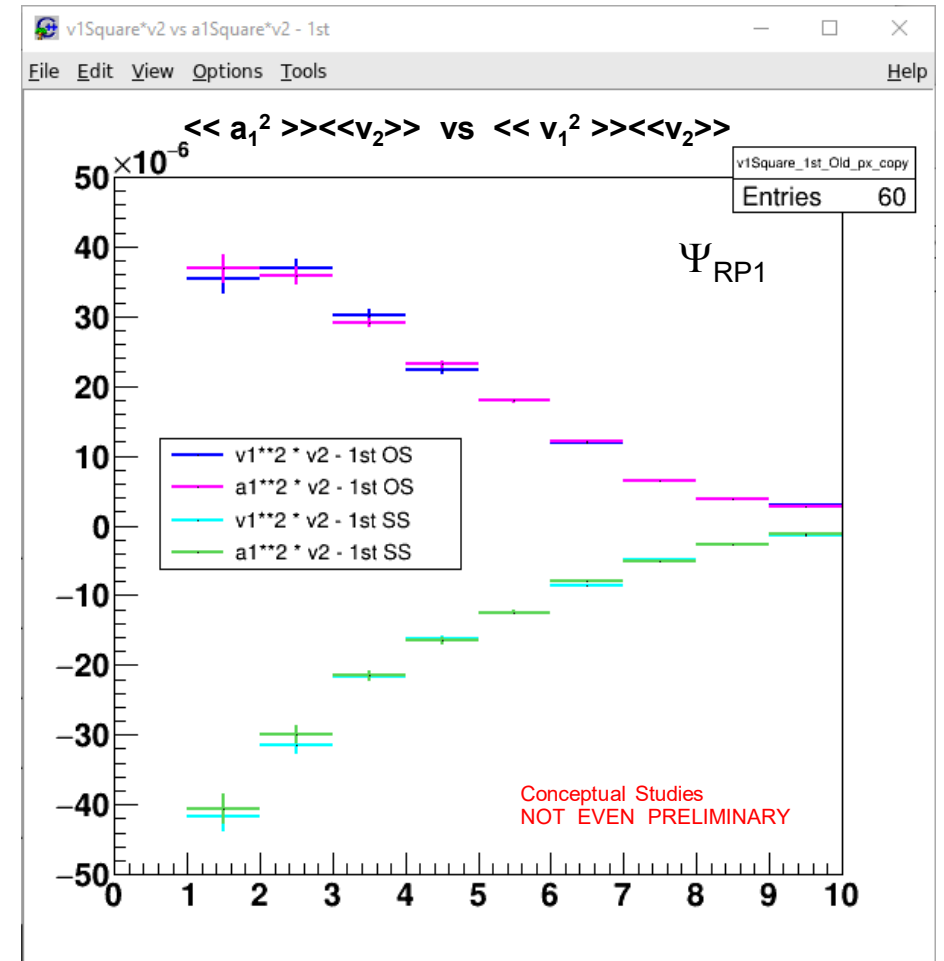
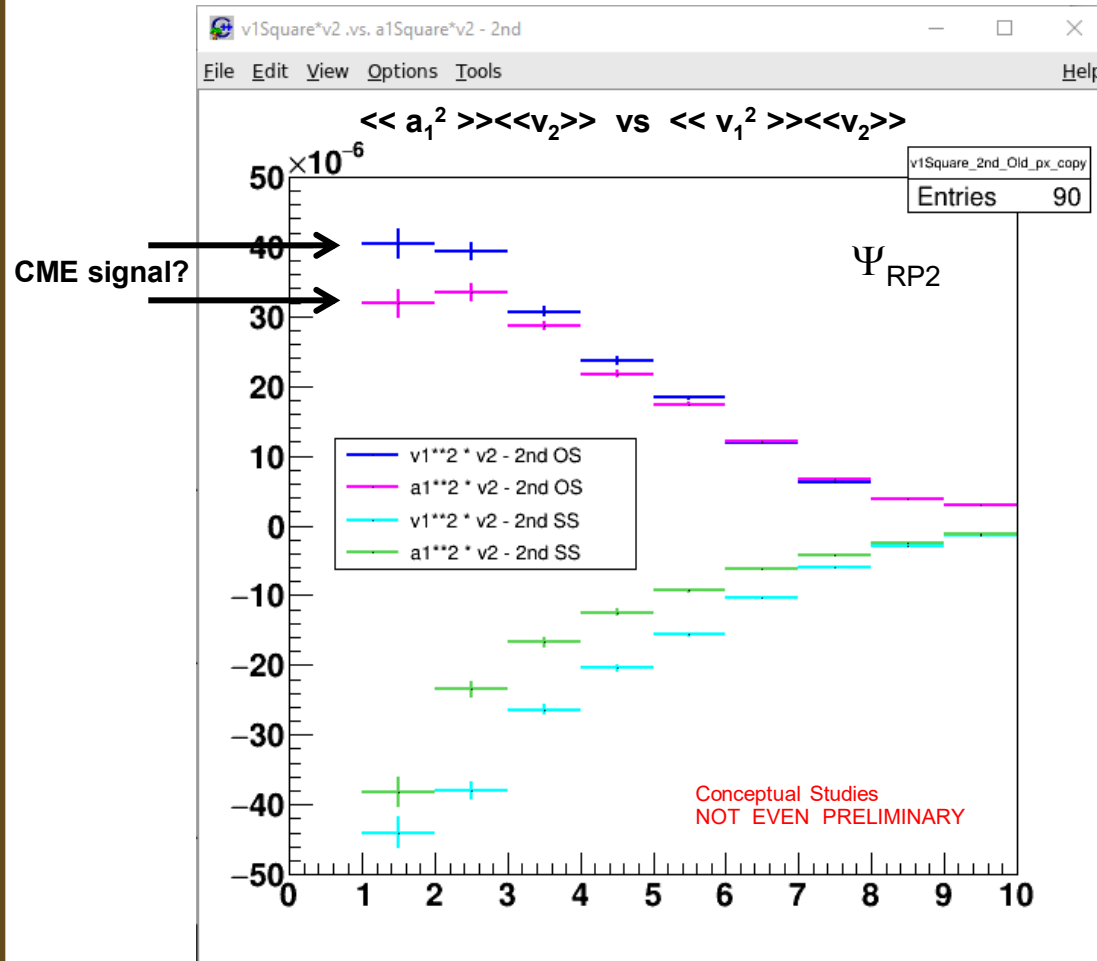
while  $(v_1^2 - a_1^2)$  with  $\Psi_{RP1}$  is  $\sim$ zero





# The Chiral Magnetic Effect

## Compare $\langle\langle a_1^2 \rangle\rangle * \langle\langle v_2 \rangle\rangle$ and $\langle\langle v_1^2 \rangle\rangle * \langle\langle v_2 \rangle\rangle$

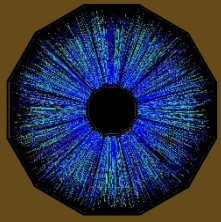


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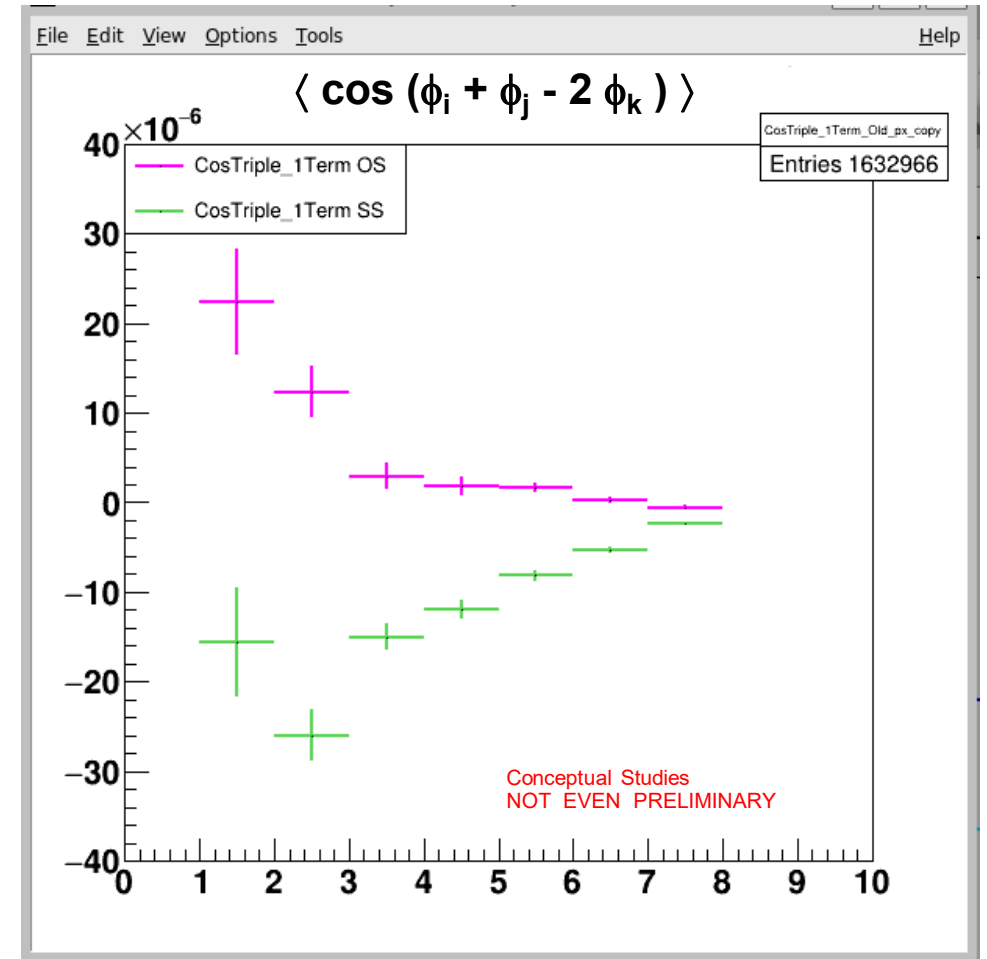
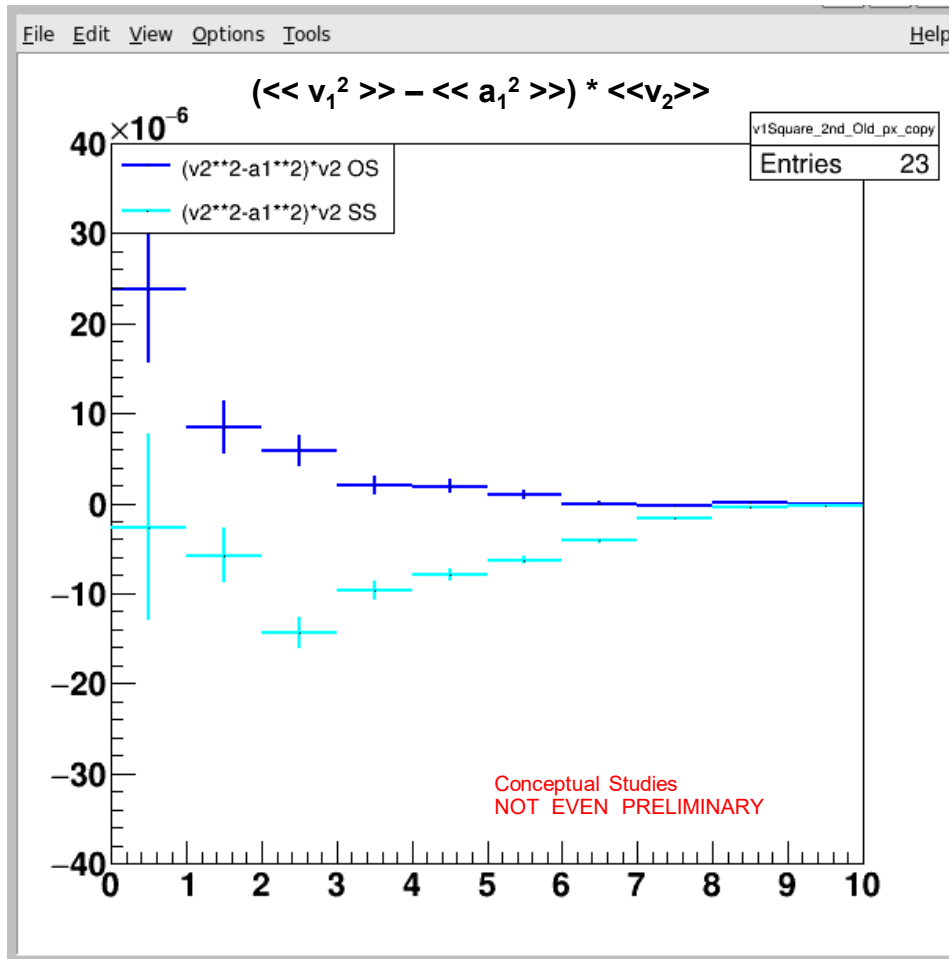
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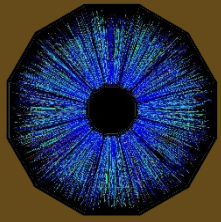
- $\langle\langle a_1^2 \rangle\rangle * \langle\langle v_2 \rangle\rangle$  is similar in shape and magnitude to  $\langle\langle v_1^2 \rangle\rangle * \langle\langle v_2 \rangle\rangle$  (note global avg)
- $\langle\langle a_1^2 \rangle\rangle * \langle\langle v_2 \rangle\rangle$  shows charge separation ... but so does  $\langle\langle v_1^2 \rangle\rangle * \langle\langle v_2 \rangle\rangle$
- I didn't expect to see that ...



# $(v_1^2 - a_1^2) * v_2$ using $\Psi_{RP2}$ in 200 GeV Au-Au (Run 19)

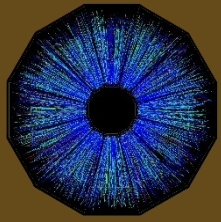


- Note that  $\langle \cos(\phi_i + \phi_j - 2\phi_k) \rangle$  was calculated on an EbyE basis,  $\Sigma (v_1^2 - a_1^2) * v_2$
- But, on this page, we are comparing it to  $(\langle v_1^2 \rangle - \langle a_1^2 \rangle) * \langle v_2 \rangle$
- The curves in the left and right figures are similar in shape and magnitude



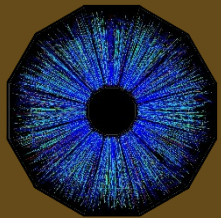
## Concluding thoughts

- $\langle\langle a_1^2 \rangle\rangle$  contains a significant amount of 'signal' (i.e. not small)
- $\langle\langle v_1^2 \rangle\rangle$  contains a significant amount of 'signal' (i.e. also, not small)
  - $\langle\langle v_1^2 \rangle\rangle$  is full of signal and similar in shape and magnitude to  $\langle\langle a_1^2 \rangle\rangle$
- Both  $\langle\langle a_1^2 \rangle\rangle$  and  $\langle\langle v_1^2 \rangle\rangle$  show charge separation with  $OS > 0$ ,  $SS < 0$ 
  - Not what we expected
- The difference between these two curves times  $\langle\langle v_2 \rangle\rangle$  is small and similar in shape and magnitude to the  $\gamma$  correlator ( $\Psi_{RP2}$ )
  - It could be the CME
- $(\langle\langle v_1^2 - a_1^2 \rangle\rangle) * \langle\langle v_2 \rangle\rangle$  includes a global average for  $v_2$  and not EbyE with the other terms, yet the product looks very similar to  $\langle\langle (v_1^2 - a_1^2) * v_2 \rangle\rangle$
- The data are not fully consistent with the assumptions put forth at the start of the talk and so we may not be isolating  $a_{1CME}$  in the way we had hoped
- Bottom line: we are putting our faith in the subtraction of two large numbers to find a small signal. This could be a risky strategy when looking for new physics.



## Technical notes

- The RPs were calculated using the TPC data, only.
- Centrality bins are preliminary, not the official Run 19 determination.
- The data for  $\langle \cos(\phi_i + \phi_j - 2\phi_k) \rangle$  in the centrality bins 0-5% and 5-10% (pg 8) have been explicitly suppressed because they are expensive to calculate in a triple correlation. These are central events and we expect the result to be zero.
- Data taken from one run (~1.8 M Evts Run 19). This is a curse and a blessing: it makes the acceptance corrections stable but results could be a statistical fluke.
- Pion data, selected by  $2\sigma$  cut on dE/dx band
- In principle,  $v_1$  and  $a_1$  should be measured wrt the 1<sup>st</sup> order reaction plane,  $v_2$  should be measured wrt the 2<sup>nd</sup> order RP. If we take the 1<sup>st</sup> order RP results seriously then the charge separation signal is zero. Would be good to do this again with a high quality measure of the 1<sup>st</sup> order RP such as the EPD
- It is computationally inefficient to calculate auto-correlations for a three particle correlation (especially when using TPC data). We could use independent 1<sup>st</sup> and/or 2<sup>nd</sup> order RP determination (e.g. the EPD) which would simplify the auto-correlation corrections. Food for thought and an obvious next step.



# The Chiral Magnetic Effect

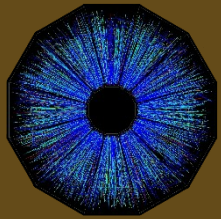
Jim Thomas

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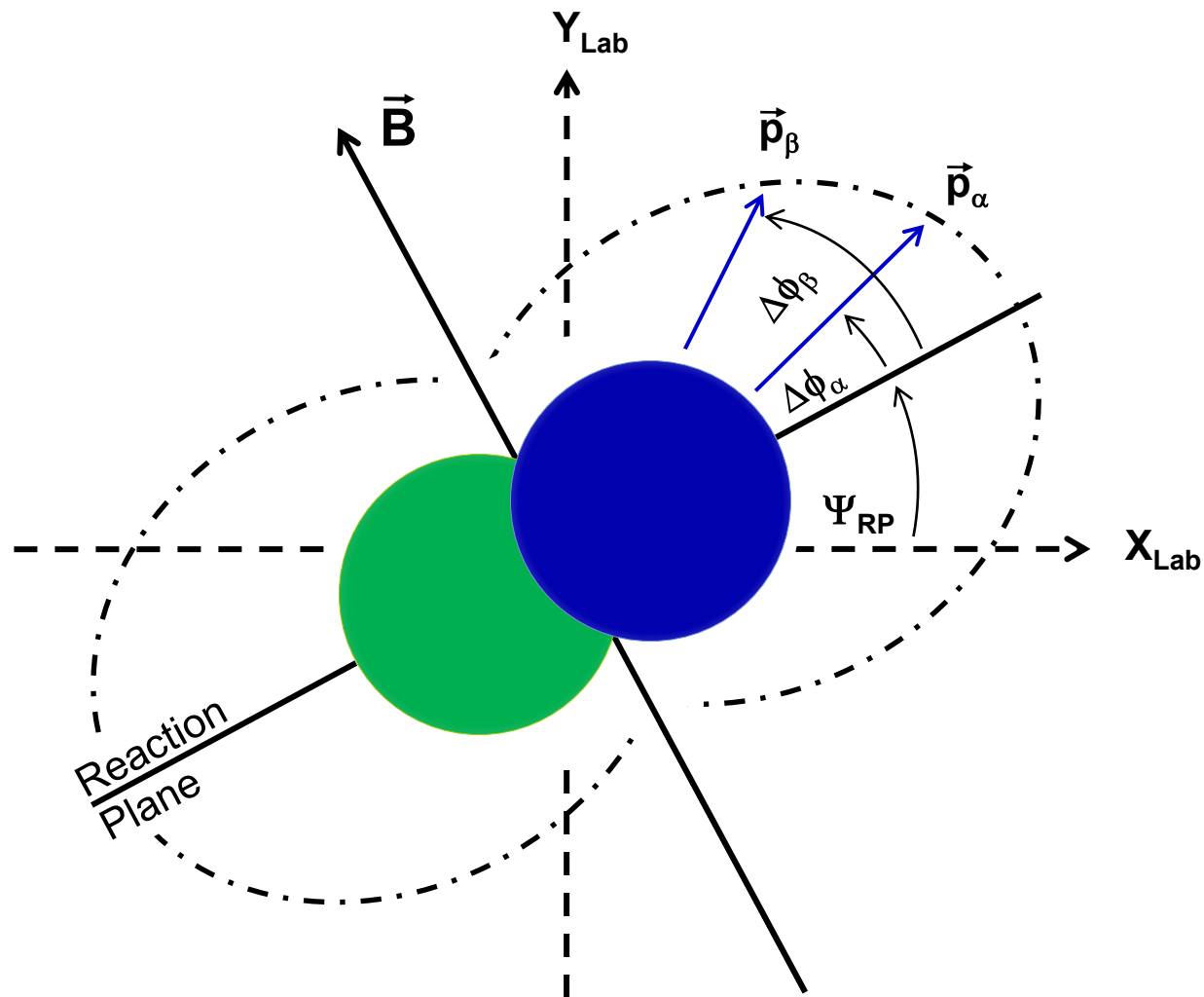
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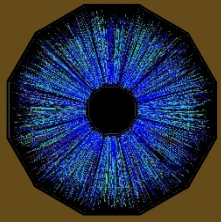
Backup Slides



## Analysis Uses Standard Flow Tools



- The line between the centers of the nuclei and the beam axis define the reaction plane – perpendicular to angular momentum vector and B field



# Full Fourier Transform of the Invariant Yield

$$f(\phi) = \frac{b'_0}{2} + \sum_{n=1}^{\infty} ( a'_n \sin(n\phi) + b'_n \cos(n\phi) )$$

where

$$a'_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(\phi) \sin(n\phi) d\phi \quad \text{for } n = 1, 2, \dots$$

$$b'_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(\phi) \cos(n\phi) d\phi \quad \text{for } n = 0, 1, 2, \dots$$

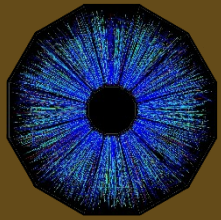
If we want to test if parity is conserved then we should keep the extra terms

$$E \frac{dN^3}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_T dp_T dy} ( 1 + \underline{2a_1 \sin(\Delta\phi)} + 2b_1 \cos(\Delta\phi) + \underline{2a_2 \sin(2\Delta\phi)} + 2b_2 \cos(2\Delta\phi) + \dots )$$

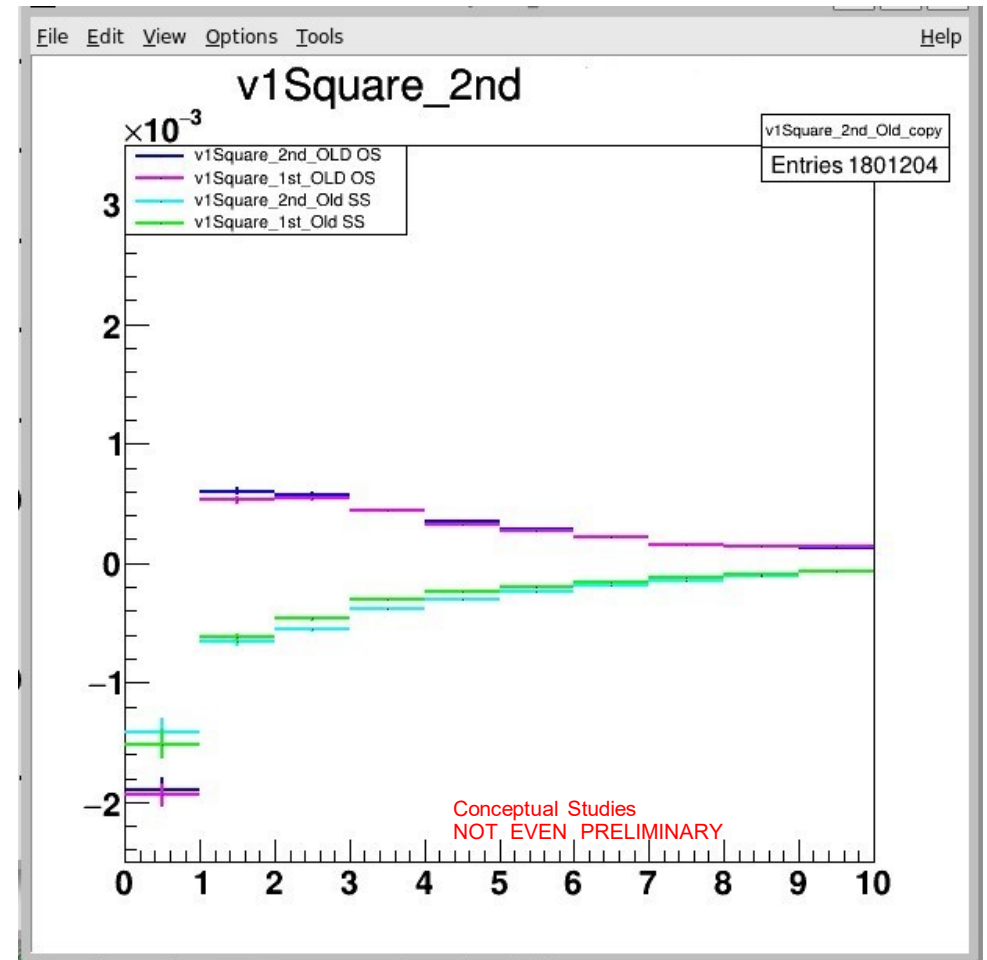
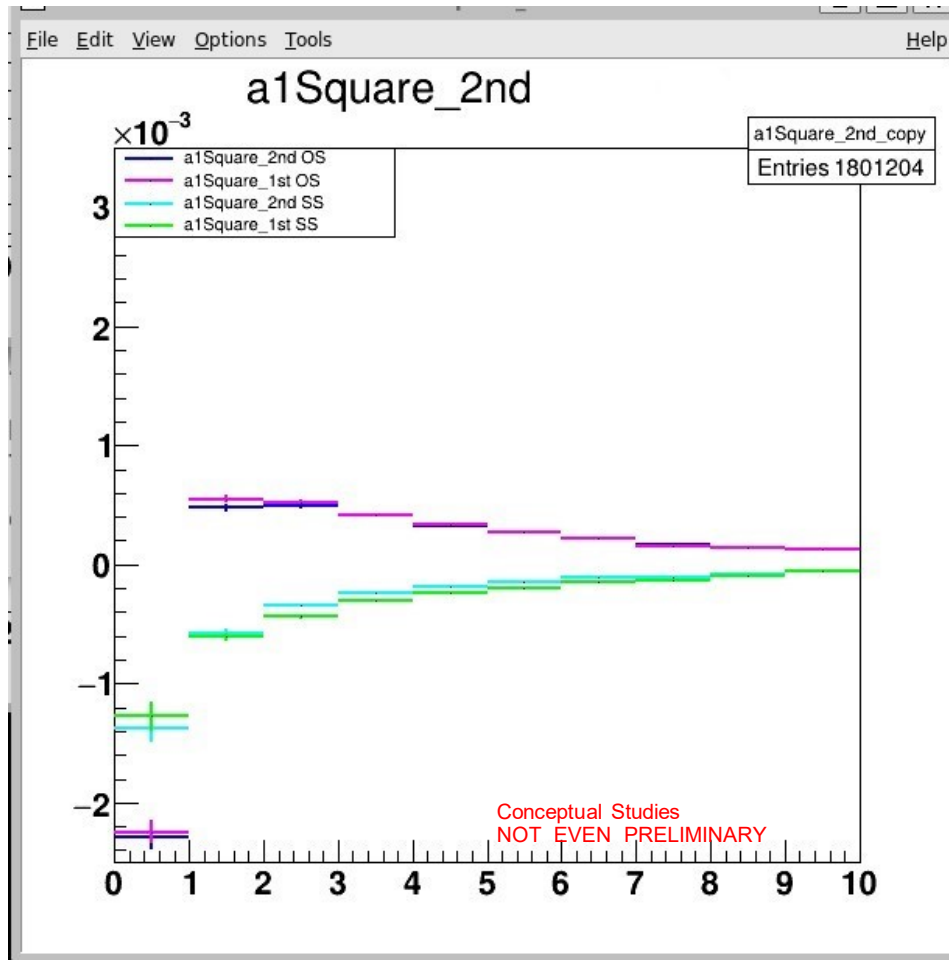
where

$$a_n = \pi a'_n = \sum_i \sin( n(\phi_i - \Psi_R) ) , \quad b_n = \pi b'_n = \sum_i \cos( n(\phi_i - \Psi_R) )$$

**The standard HI flow analysis assumes  $a = 0$  and assigns  $b_n \equiv v_n$**



# $a_1^2$ and $v_1^2$ from the 200 GeV Au-Au Run 19



- The notation  $a_1^2$  denotes the EbyE quantity  $\Sigma (a_{1,p1} * a_{1,p2})$  with  $p1 \neq p2$
- $a_1^2$  shows charge separation ... but so does  $v_1^2$  ... I didn't expect to see that